

Functional Programming Makes a Comeback

Chuck Allison

Better Software 2008

Observation

- Popular object-oriented languages have some degree of support for functional programming
 - Python, Ruby, C++, Java, C#, D, F#, Scala, Groovy
- C++, Java, and C# are adding even more support
- What's so cool about FP?

Objective

- To appreciate the contribution the functional style of programming makes to problem solving
- To become familiar with the functional style of programming in modern languages

Agenda

- What is Functional Programming?
- History of FP
- **ML** – The first Modern FP Language
- FP in Other Modern Languages
 - Python, D, C++, Scala, C#

What is Functional Programming?

The First Programming Language!

Functional Programming

- A style (paradigm) of programming where **functions** are the basic building blocks
 - Functions are used for what they *return*
 - *Not* for achieving side effects (e.g., *assignment*)
- Functions are “first-class” entities
 - Can be passed as arguments, returned as results
 - Can be created “on-the-fly”
- FP programs focus more on *what* you want
 - Not so much on *how* to compute it

Key FP Features

- Higher-order functions
 - Functions can be passed and returned
- Nested functions
 - With *closures* (a type of delegate)
- Partial function application
 - Aka “currying”
- No assignment statement
 - High-level (and thread-safe) programming
- No loops
 - Recursion preferred

History of Functional Programming

Before Computers...

- ...there was *computation*
- Mathematical operations and functions
- Symbolic manipulation
 - a key focus of 20th Century mathematics

Great Moments in Computation

- Turing Machines
 - Where imperative programming originated
 - Led to FORTRAN, Algol, C, etc.
- Church's Lambda Calculus
 - Led to Lisp, Scheme, ML, Haskell, etc.
- Both happened in the 1930s!

Milestones in Functional Programming

- 1936 – Church’s Lambda Calculus
- 1958 – First release of Lisp
- Early 1970s – ML
 - Static typing
 - Type inference
 - Function templates (“parametric polymorphism”)
- Mid 1970’s – Scheme (Lisp for the masses)
 - Block scoping; tail recursion optimization
- 1990 – Haskell (**S**oftware **T**ransactional **M**emory)
- 1998 – Erlang (Fault tolerant, Message Passing)

Introduction to ML

The First Modern Functional Programming Language

ML Topics

- Getting Started
 - Types, Expressions, Bindings
 - Functions, Type Inference, Tuples
- Lists and Recursion
 - List operations, Pattern-Matching, Type Variables
- Higher-order Functions
 - Lambda expressions (anonymous functions)
 - Currying, Folding
 - Nested Functions and Closures

The ML Interpreter

```
$ sml
Standard ML of New Jersey v110.67 [built: Thu Nov 15 10:18:08
2007]
- 1 + 2;
val it = 3 : int
- 1 - 2;
val it = ~1 : int
- "the" ^ "end";
val it = "theend" : string
- 2.0 + 3.0;
val it = 5.0 : real
- 2.0 + 5;
stdIn:5.1-5.8 Error: operator and operand don't agree [literal]
  operator domain: real * real
  operand:          real * int
  in expression:
    2.0 + 5
```

```
- #"a";
val it = #"a" : char
- 1 = 2;
val it = false : bool
- 1 > 2 andalso 3 > 2;
val it = false : bool
- 1 < 2 orelse 3 > 2;
val it = true : bool
- 1.0 = 2.0;
stdIn:9.1-9.10 Error: operator and operand don't agree
[equality type required]
  operator domain: 'tZ * 'tZ
  operand:          real * real
in expression:
  1.0 = 2.0
```

```
- true orelse 1 div 0 = 0;
val it = true : bool
- if 1 > 0 then "greater" else "not"; (* an expression *)
val it = "greater" : string
- 2 / 5;
stdIn:11.1-11.6 Error: operator and operand don't agree
[literal]
  operator domain: real * real
  operand:          int * int
  in expression:
    2 / 5
- 2.0 / 5.0;
val it = 0.4 : real
- 2 div 5;
val it = 0 : int
```


Basic ML Types

- `int`
- `real`
 - Not an “equality type”
 - Can’t mix with **`int`**
- `string`
- `char`
- `bool`
 - **`andalso`** and **`orelse`** are *short-circuiting*

Binding Variables

- **val** keyword
- The type of the initializer expression becomes the type of the initialized variable
 - “type inference”
- It’s not really “variable”
 - i.e., it’s not mutable
 - can only be **initialized**
- But variables can be “rebound”

Variable Bindings

```
- val n = 2;  
val n = 2 : int  
- val m = n + 1;  
val m = 3 : int  
- val n = 10;  
val n = 10 : int  
- m;  
val it = 3 : int
```



Basic Operators

- For Integers:
 - +, -, *, div, mod, ~
- For Reals:
 - +, -, *, /, ~
- For Strings:
 - ^ (concatenation)

Functions in ML

- ML functions take exactly 1 argument
- That argument can be an aggregate
 - tuple, list, etc.
- Parentheses not needed:
 - `f x;`

Calling Functions in ML

```
- floor 2.5;
val it = 2 : int
- real 2;
val it = 2.0 : real
- explode "hello";
val it = [#"h",#"e",#"l",#"l",#"o"] : char list
- implode [#"h",#"e",#"l",#"l",#"o"];
val it = "hello" : string
- floor 2.6 + 1;
val it = 3 : int
- floor (2.6 + 2.0);
val it = 4 : int
```

Commonly Used Functions

- Numeric conversions:
 - real, floor, ceil, round, trunc
- Character-to-integer conversion:
 - chr, ord
- Character-to-string conversion:
 - str, explode, implode

Defining Functions in ML

```
- fun square x = x * x;  
val square = fn : int -> int  
- square 2;  
val it = 4 : int  
- square 2 + 2;  
val it = 6 : int  
- square (2 + 2);  
val it = 16 : int
```


Annotating Functions with Types

```
- fun square x:real = x*x;      (* annotate argument type *)
val square = fn : real -> real
- square 2;
stdIn:2.1-2.9 Error: operator and operand don't agree [literal]
  operator domain: real
  operand:          int
  in expression:
    square 2
- square 2.0;
val it = 4.0 : real
- square (real 2);              (* Note paren placement! *)
val it = 4.0 : real
- fun square (x:real):real = x*x; (* annotate return type *)
val square = fn : real -> real
```

Defining Functions in ML

- **fun** keyword
- function name
- single parameter = expression;
- - `fun max (x,y) = if x > y then x else y;`
`val max = fn : int * int -> int`

`(x,y)` is a *tuple*

Tuples

- Can hold an *arbitrary number* of elements
 - *Of any type*
- Accessed positionally with #1, #2, etc.
- Can perform tuple assignment

Tuple Access and Assignment

```
- val twonums = (2,3);  
val twonums = (2,3) : int * int  
- #1 twonums;  
val it = 2 : int  
- #2 twonums;  
val it = 3 : int  
- val (x,y) = twonums;  
val x = 2 : int  
val y = 3 : int  
- x = #1 twonums;  
val it = true : bool
```

Summary

Getting Started with ML

- ML is *strongly typed*
 - no mixing of types in expressions
 - types are statically determined
- Variables are *bound to values*
 - the value can't be changed
 - but the variable can be rebound to another value
- Functions take a *single argument* and return a *single value*
 - Function bodies are a *single expression*

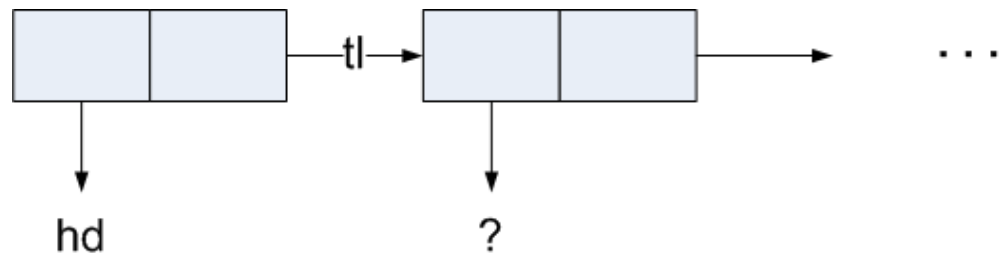
Exercises

Getting Started

- Write an ML function that takes a real number and returns its cube (3rd power)
- Write an ML function that returns the smallest of 3 integers
- Write an ML function that returns the sum of its 3 integer arguments

Lists in ML

- Must be homogeneous
 - i.e., each element must be of the same type
- Stored as linked lists of pairs of pointers
 - first element is the *head* (refers to a value)
 - second element is the *tail* (refers to rest of list)
 - is itself a list



Using Lists

```
- val a = [1,2,3];  
val a = [1,2,3] : int list  
- hd a;  
val it = 1 : int  
- tl a;  
val it = [2,3] : int list  
- hd (tl a);  
val it = 2 : int  
- null a;  
val it = false : bool  
- null [];  
val it = true : bool  
- nil;  
val it = [] : 'a list
```


Basic List Operations

- Concatenation: **@**
 - $[1,2] @ [3,4] \Rightarrow [1,2,3,4]$
- Construct a node: **::**
 - $1::[2,3,4] \Rightarrow [1,2,3,4]$
- Determine head: **hd**
 - $hd [1,2,3,4] \Rightarrow 1$
- Determine tail: **tl**
 - $tl [1,2,3,4] \Rightarrow [2,3,4]$
- Length: **length**

Writing List-processing Functions

- Done with *recursion* to visit each list element
- Typical pattern:
 - if list is empty
 process base case of recursion
 - else
 process head, recurse on tail

Writing a Length Function for Lists

```
fun mylen x =  
  if null x then 0  
  else 1 + length (tl x);
```

Another Recursive Function

```
(* Sum of squares of 0 through n *)
- fun sumsq n =
=     if n = 0 then 0
=     else n*n + sumsq (n-1);
val sumsq = fn : int -> int
- sumsq 2;
val it = 5 : int
- sumsq 3;
val it = 14 : int
```

Pattern Matching

```
- fun sumsq 0 = 0
= |   sumsq n = n*n + sumsq (n-1);
val sumsq = fn : int -> int
- sumsq 2;
val it = 5 : int
- sumsq 3;
val it = 14 : int
- sumsq 0;
val it = 0 : int
```

mylen with Pattern Matching

```
- fun mylen nil = 0
= |   mylen (h::t) = 1 + mylen t; (* h is not used *)
val mylen = fn : 'a list -> int   (* a type variable *)
- mylen [];
val it = 0 : int
- mylen [1,2,3];
val it = 3 : int
```

Unused Variables

- If a variable won't be used, you can use the *underscore* for its name:

```
|    mylen (_::t) = 1 + mylen t;
```

- This applies in other contexts:

```
- var (_,y) = (1,2);  
val y = 2 : int
```

Type Variables

- Notice the ' **a** ' in the definition of `mylen`
- The operations of `mylen` are *type independent*
- Therefore, the type of the list can *vary*
 - `mylen ["hello", "goodbye"];`
`val it = 2 : int`
- This is a form of *polymorphism*
 - “Parametric Polymorphism”
 - The inspiration for C++ function templates
- The type is fixed when the statement is *compiled*

Testing For List Membership

```
- fun member (_, nil) = false
= |   member (x, h::t) = x = h orelse member (x,t);
stdIn:27.26 Warning: calling polyEqual (* Ignore this *)
val member = fn : 'a * 'a list -> bool
- member (2,[1,2]);
val it = true : bool
- member (3,[1,2]);
val it = false : bool
- member (1, nil);
val it = false : bool
```

The ' 'a Type Variable

- Remember that reals can't be compared for equality
- The `member` function requires equality types
- The type variable ' 'a stands for any equality type
 - can't call this function on a list of reals!

Multiple Type Variables

```
- fun outer (x,_,z) = (x,z);  
val outer = fn : 'a * 'b * 'c -> 'a * 'c  
- outer (1,2,3);  
val it = (1,3) : int * int  
- outer ("a","b","c");  
val it = ("a","c") : string * string
```

Reversing a List

```
- fun reverse nil = nil
= |   reverse (h::t) = reverse t @ [h];
val reverse = fn : 'a list -> 'a list
- reverse [1,2,3];
val it = [3,2,1] : int list
- rev ["a","b","c"];    (* built-in function *)
val it = ["c","b","a"] : string list
```

Defining Local Variables

- The only locals we've seen are parameters
- The **let** expression defines local bindings
- They are used in the function body
 - Which is a single expression, remember

The let Expression

```
- fun days2ms days =  
=   let  
=       val hours = days * 24.0  
=       val minutes = hours * 60.0  
=       val seconds = minutes * 60.0  
=   in  
=       seconds * 1000.0  
= end;  
val days2ms = fn : real -> real  
- days2ms 1.5;  
val it = 129600000.0 : real
```

A Local Function Definition

```
fun union (x, nil) = x
| union (x, head::rest) =
  let
    fun member (_, nil) = false
    | member (x, h::t) = x = h orelse member (x,t)
  in
    if member(head, x) then union(x,rest)
    else head::union(x,rest)
  end;
```

```
- union (["a","b","c"],["b","c","d"]);
val it = ["d","a","b","c"] : string list
```

Summary

Lists and Recursion

- Lists have a head and a tail
 - the empty list is denoted by **nil**
- Patterns are matched in the order they appear
- ML allows parametric polymorphism
 - implicit type variables
- Place local bindings in a **let** block

Exercises

Lists and Recursion

- Write a function named **repeats** that determines if a list has two adjacent equal elements
- Write a function named **unique** that returns elements of a sorted list but ignoring duplicates.
- After reviewing the code or union, write a binary function named **intersection**, that returns only those elements common to both its input lists.

Functions are First-Class Entities

- Functions are like other values in that:
 - they can be *passed* as arguments to other functions
 - they can be *returned* from functions
 - they can be *bound* to variables
- A function that accepts or returns another function is called a *higher-order* function
 - very useful!

Using Functions as Objects

```
- length;  
val it = fn : 'a list -> int  
- val f = length;  
val f = fn : 'a list -> int  
- fun apply (f,x) = f x;  
val apply = fn : ('a -> 'b) * 'a -> 'b  
- apply (f, [1,2,3]);  
val it = 3 : int
```

Using Operator Functions

```
- op <;  
val it = fn : int * int -> bool  
- (op <) (3,4);  
val it = true : bool  
- val g = op <;  
val g = fn : int * int -> bool  
- g(4,3);  
val it = false : bool
```

Quicksort in ML

```
fun quicksort (cmp, nil) = nil
| quicksort (cmp, pivot::rest) =
  let
    fun partition nil = (nil, nil)
    | partition(x::xs) =
      let
        val (below, above) = partition xs
      in
        if cmp(x, pivot) then (x::below, above)
        else (below, x::above)
      end;
    val (below, above) = partition(rest)
  in
    quicksort(cmp, below) @ [pivot] @ quicksort(cmp, above)
  end;
```

Using Quicksort

```
- val words = ["go", "ahead", "make", "my", "day"];  
val words = ["go", "ahead", "make", "my", "day"] : string list  
- quicksort(String.<, words);  
val it = ["ahead", "day", "go", "make", "my"] : string list  
- quicksort(String.>, words);  
val it = ["my", "make", "go", "day", "ahead"] : string list
```

Anonymous Functions

- Called *lambda expressions* in other FP languages
- Sometimes it is more convenient to create a function on the fly
- Uses **fn arg => expr** syntax

```
- quicksort(fn (x,y) => x < y, [3,2,1]);  
val it = [1,2,3] : int list  
- quicksort(fn (x,y) => x > y, [1,2,3]);  
val it = [3,2,1] : int list
```

Currying

- Named after Haskell Curry
- A flexible way of providing *multiple arguments* to a functions
- Allows *partial function evaluation*
 - So you can provide the other arguments later
- Technique:
 - For all but the last parameter, *a function is returned* that takes the next parameter
 - The last returned function returns the actual value

Currying Syntax

```
- fun f a = fn b => a + b;  
val f = fn : int -> int -> int  
- f 1;  
val it = fn : int -> int  
- f 1 2;  
val it = 3 : int  
- val g = f 1;  
val g = fn : int -> int  
- g 2;  
val it = 3 : int
```

Currying Shorthand

```
- fun f a b = a + b;  
val f = fn : int -> int -> int  
- f 1;  
val it = fn : int -> int  
- f 1 2;  
val it = 3 : int  
- val g = f 1;  
val g = fn : int -> int  
- g 2;  
val it = 3 : int
```

A Curried Quicksort

```
fun quicksort cmp L = if null L then nil else
  let
    val (pivot, rest) = (hd L, tl L)
    fun partition nil = (nil, nil)
      | partition(x::xs) =
        let
          val (below, above) = partition xs
        in
          if cmp(x, pivot) then (x::below, above)
          else (below, x::above)
        end;
    val (below, above) = partition(rest)
  in
    quicksort cmp below @ [pivot] @ quicksort cmp above
  end;
```

Using the Curried Quicksort

```
- use "/Users/chuck/sort2.sml";
[opening /Users/chuck/sort2.sml]
val quicksort = fn : ('a * 'a -> bool) -> 'a list -> 'a list
val it = () : unit
- val sortasc = quicksort (op <);
val sortasc = fn : int list -> int list
- sortasc [3,2,1];
val it = [1,2,3] : int list
- sortasc [5,4,3];
val it = [3,4,5] : int list
- val sortdesc = quicksort (op >);
val sortdesc = fn : int list -> int list
- sortdesc [1,2,3];
val it = [3,2,1] : int list
- sortdesc [3,4,5];
val it = [5,4,3] : int list
```

Standard Higher-Order Functions

- **map**
 - Applies a unary function to each list element
 - Returns the resulting list
- **foldl**
 - Reduces a list to a value
 - Applies a binary function to each element with the accumulated value
 - Works left-to-right
- **foldr**
 - Like **foldl** but works right-to-left
- All are *curried*

Using map

```
- map;  
val it = fn : ('a -> 'b) -> 'a list -> 'b list  
- map (fn x => x + 1) [1,2,3];  
val it = [2,3,4] : int list  
- val add1 = map (fn x => x + 1);  
val add1 = fn : int list -> int list  
- add1 [1,2,3];  
val it = [2,3,4] : int list  
- add1 [2,3,4];  
val it = [3,4,5] : int list  
  
- map (op +) [(1,2), (3,4), (5,6)];  
val it = [3,7,11] : int list
```

Using foldl

```
(* Add list elements *)  
- foldl (op +) 0 [1,2,3]; (* (((0+1)+2)+3), or... *)  
val it = 6 : int (* op+(3,op+(2,op+(1,0))) *)
```

```
(* Multiply them *)  
- foldl (op * ) 1 [2,3,4]; (* op*(4,op*(3,op*(2,0))) *)  
val it = 24 : int
```

```
(* Sum of squares: f(3,f(2,f(1,1))) *)  
- foldl (fn (x,sofar) => sofar + x*x) 0 [1,2,3];  
val it = 14 : int
```

Leveraging Currying

```
- val addup = foldl (op +) 0;
val addup = fn : int list -> int
- addup [1,2,3];
val it = 6 : int
- addup [2,3,4];
val it = 9 : int
- val concat = foldl (op ^) "";
val concat = fn : string list -> string
- concat ["how", "now", "brown", "cow"];
val it = "cowbrownowhow" : string
```


Using foldr

```
- val concat = foldr (op ^) "";  
val concat = fn : string list -> string  
- concat ["how", "now", "brown", "cow"];  
val it = "hownowbrowncow" : string  
- val append5 = foldr (op ::) [5];  
val append5 = fn : int list -> int list  
- append5 [1,2,3];  
val it = [1,2,3,5] : int list
```

Question

- **append5** is a little too specific
- How can we write a *generic append*?
 - i.e., build **append(n)** on-the-fly

A Generic append

```
- fun append n = foldr (op ::) [n];  
val append = fn : 'a -> 'a list -> 'a list  
- val append3 = append 3;  
val append3 = fn : int list -> int list  
- append3 [0,1,2];  
val it = [0,1,2,3] : int list
```

Nested Functions and Closures

- **append3** made a *partial call* to **append**
 - A *function*, not a value, was returned
- The returned function used a binding from *outside* of its scope (**n**)
- The binding for **n** needs to be available after **append** returns
- What **append** actually returned is a *closure*
 - a function coupled with its *lexical environment*

More Examples

```
- fun bor bools = foldr (fn (a, b) => a orelse b) false bools;
val bor = fn : bool list -> bool
- bor [false,true,false];
val it = true : bool
- fun member x L = bor (map (fn y => x = y) L);
stdIn:82.5 Warning: calling polyEqual
val member = fn : 'a -> 'a list -> bool
- member 5 [3,4,5];
val it = true : bool
```

Design Exercise: Function Composition

- Data processing is often *a sequence of transformations* on data
 - e.g., remove punctuation, then change to lower case, then change all e's to 3's
- Packaging a sequence of functions into a single, composite function is called *function composition*
- **f (s) <==> threes (lower (nopunct (s)))**
- Just as currying allows reuse of a partially-evaluated function, composition allows a *sequence of operations* to be *reused as a unit*

Solution Approach

- We will be given a list of unary functions
 - This example requires the input and output types to be the same
- We need to return a unary function that applies each original function in reverse list order to obtain the final result
- Sounds like a job for lists and **foldr**

Using compose

```
use "/Users/chuck/compose.sml";
val compose = fn : ('a -> 'a) list -> 'a -> 'a
val it = () : unit
- fun add1 x = x + 1;
val add1 = fn : int -> int
- fun mult3 x = x*3;
val mult3 = fn : int -> int
- fun sub5 x = x - 5;
val sub5 = fn : int -> int
- val f = compose [add1,mult3,sub5];
val f = fn : int -> int
- f(1) ;
val it = ~11 : int
- f(20);
val it = 46 : int
```


Implementing compose

```
fun compose flist =  
  fn x => foldr (fn (f, sofar) => f sofar) x flist;
```

We'll see this again in other languages...

FP Summary So Far

- Variables do not change
 - no *shared memory* problems (globals, threads, etc.)
- No loops
 - => no loop errors
 - use recursion instead
- Very high-level programming
 - facilitated by higher-order functions, anonymous functions, nested functions, currying
 - concise code!

FYI

- **OCaml** is an object-oriented ML
- Compiles to native code
 - runs very fast!
- Supports procedural, functional, and OO programming
- **F#** on .NET

Exercises

Higher-Order Functions

- Write a curried version of **union**; use **foldl** or **foldr**
- Repeat for **intersection**
- Write a curried version of **append**
 - Hint: use **foldr**; then “cons” (::) elements of the first list with the second

Functional Programming in Other Languages

Topics

Other Languages

- FP in Python
- FP in D
- FP in C++
- FP in Scala

About Python

- Python is a *dynamically typed* language
 - there is no “compile time”
 - dynamic OO programming
- Interpreted (but no JIT compiler)
- Easy to learn, read
 - indentation is *required*
- Lists and tuples are *indexable*
 - Lists are *mutable*; tuples are not

Lists in Python

```
>>> L=[1,2,2,3,3,3]
>>> for n in L: print L.count(n) ,
1 2 2 3 3 3
>>> L.index(2)
1
>>> L.append(5)
>>> L
[1, 2, 2, 3, 3, 3, 5]
>>> L.extend([5,5,5,5])
>>> L
[1, 2, 2, 3, 3, 3, 5, 5, 5, 5, 5]
>>> for i in range(4): L.insert(6+i, 4)
>>> L
[1, 2, 2, 3, 3, 3, 4, 4, 4, 4, 5, 5, 5, 5, 5]
```


Slices

```
words = "now is the time".split()
print words
print words[1]
print words[0:2]
print words[1:]
print words[:2]
print words[-1]
```

```
''' Output:
['now', 'is', 'the', 'time']
is
['now', 'is']
['is', 'the', 'time']
['now', 'is']
time
'''
```

Defining Functions in Python

- **def** keyword
- Arguments can be *collected* into a *tuple parameter*
- Tuples can be *flattened* into arguments
- Python supports *nested functions* and *closures*

Functions in Python

```
def h(x):  
    return x + 2
```

```
def r(s):  
    return s*2
```

```
# g calls f on x:  
def g(f, x):  
    return f(x)
```

```
print g(h,3)           # prints 5  
print g(r,'two')      # prints twotwo  
#print g(2,3)         # error: 2 is not callable
```

Arguments and Tuples

```
def varargs(*args):  
    for arg in args:  
        print arg
```

```
varargs("one", "two")  
varargs(3, 4, 5)
```

```
''' Output:
```

```
one
```

```
two
```

```
3
```

```
4
```

```
5
```

```
'''
```

```
def fixargs(a,b):  
    print 'a =', a  
    print 'b =', b
```

```
pair = (1, "two")  
fixargs(*pair)
```

```
''' Output:
```

```
a = 1
```

```
b = two
```

```
'''
```

Quicksort in Python

Uses List Comprehensions

```
def qsort(L):  
    if len(L) <= 1: return L  
    return qsort([lt for lt in L[1:] if lt < L[0]]) \  
        + [L[0]] \  
        + qsort([gt for gt in L[1:] if gt >= L[0]])
```

FP in Python

- **map** = same as ML
- **foldl** = **reduce**
- There is no **foldr**
 - but you can easily traverse lists backwards with the **reversed** iterator
- Currying is not directly supported
 - easily provided with a 7-line “wrapper” function

Python FP Examples

```
>>> map(lambda x: -x, [1,2,3])
[-1, -2, -3]
>>> [-x for x in [1,2,3]]
[-1, -2, -3]
>>> map(lambda x,y: x+y, [1,2,3],[4,5,6])
[5, 7, 9]
>>> map(operator.add, [1,2,3],[4,5,6])
[5, 7, 9]
>>> reduce(operator.add, map(lambda x: -x, [1,2,3]))
-6
>>> [reduce(operator.add, x) for x in [(1,2), (3,4)]]
[3, 7]
>>> [x for x in [1,2,3] if x > 2]
[3]
```

compose in Python

```
def compose(*funs):  
    return lambda x: reduce(lambda z, f: f(z), \  
        reversed(funs), x)
```

```
def add1(x):  
    return x + 1
```

```
def mult3(x):  
    return x * 3
```

```
def sub5(x):  
    return x - 5
```

```
f = compose(add1, mult3, sub5)  
print f(1)          # -11  
print f(20)         # 46
```


Exercise

The Last One!

- Implement **union** in Python
 - takes the two sets as input
- Implement **addn** in Python
 - use it to add 5 to an existing integer list, returning a new list

The D Programming Language

- A “Modern C++”
 - higher-level, cleaner syntax
- Supports systems programming
 - and generates native executables
- Garbage collected
- Other features
 - automated unit testing
 - contract programming
 - Python-like module system
 - FP!

Introducing D

A Word Count Program (output on next slide)

```
void wc(string filename) {
    auto words = split(cast(string) read(filename));
    int[string] counts;
    foreach (word; words)
        ++counts[word];
    foreach (w; counts.keys.sort)
        writefln("%s: %d", w, counts[w]);
}

// A simple driver: process all files arguments
void main(string[] args) {
    foreach(f; args[1..$]) { // Start at second arg ([1])
        writefln("\n%s:", f);
        wc(f);
    }
}
```

```
wc.txt:
%d",: 1
([1]): 1
(f,: 1
(w,: 1
(word,: 1
++counts[word];: 1
//: 2
=: 1
all: 1
arg: 1
w,: 1
wc(f);: 1
wc(string: 1
words: 1
words): 1
writefln("%s": 1
writefln("\n%s":, 1
{: 3
}: 3
```

FP in D

- Does not have **map**, **foldr**, or **foldl**
 - but it has **foreach** and **foreach_reverse**
- Supports *nested functions* and *closures*
 - Closures in D are called *delegates*
 - Delegates couple a function with either an *enclosing function*, an *object*, or a *class*

compose in D

non-generic

```
alias int function(int) F;
alias int delegate(int) D;

D compose(F[] funs) {
    int doit(int n) {
        int result = n;
        foreach_reverse (f; funs)
            result = f(result);
        return result;
    }
    return &doit;
}
```

Using compose

```
void main() {  
    F[] funcs;  
    funcs ~= function int(int x){return x+1;};  
    funcs ~= function int(int x){return x*3;};  
    funcs ~= function int(int x){return x-5;};  
    auto c = compose(funcs); // type inference  
    writeln(c(1));          // -11  
    writeln(c(20));        // 46  
}
```

A Generic compose

```
T delegate(T) compose(T) (T function(T) [] funks)
{
    T doit(T n) {
        T result = n;
        foreach_reverse (f; funks)
            result = f(result);
        return result;
    }
    return &doit;
}
```


Using the Generic compose

```
void main() {  
    string function(string)[] sfuns;  
    sfuns ~= function string(string s) {return s ~ 's';};  
    sfuns ~= function string(string s) {return s[1..$];};  
    auto c2 = compose(sfuns);  
    writeln(c2("stale"));    // tales  
}
```

FP in C++

- Uses *function objects*
 - objects with a function-call *operator* (**operator()**)
 - the object's data constitutes the “closure”
- **map = transform**
- **foldl = accumulate**
- “Lists” can be arrays, vectors, linked-lists, etc.
 - any STL-conforming “sequence”
- 50+ sequence algorithms in the standard library

Defining a C++ Function Object

```
#include <algorithm>
#include <iostream>
using namespace std;

class addn {
    int n;
public:
    addn(int n) : n(n) {}
    int operator()(int x) {
        return x + n;
    }
};
```

Using addn

```
int main() {
    addn add5(5);
    cout << add5(10) << endl;           // 15

    int a[] = {1,2,3,4,5};
    transform(a, a+5, a, addn(10)); // 11 12 13 14 15
    for (int i = 0; i < 5; ++i)
        cout << a[i] << ' ';
    cout << endl;
}
```

Selected C++ Function Objects

Predicates

equal_to
not_equal_to
greater
less
greater_equal
less_equal
logical_and
logical_or
logical_not

Arithmetic

plus
minus
multiplies
divides
modulus
negate

A Simple Filter

```
// Add an input integer to each number in a file
```

```
int main(int argc, char* argv[]) {  
    int n = 0;  
  
    // Get n from command line  
    if (argc > 1)  
        n = atoi(argv[1]);  
  
    ifstream inf("nums.dat");  
    ofstream outf("nums.out");  
    transform(istream_iterator<int>(inf),  
              istream_iterator<int>(),  
              ostream_iterator<int>(outf, " "),  
              bind2nd(plus<int>(), n));  
}
```

Using accumulate

```
int main() {
    int a[] = {1,2,3,4};
    cout << accumulate(a, a+4, 0) << endl;

    string s[] = {"eat","my","dust"};
    string result = accumulate(s, s+3, string());
    cout << result << endl;

    cout << accumulate(a,a+4,1,multiplies<int>()) << endl;
}
```

/ Output:*

10

eatmydust

24

**/*

compose in C++

```
typedef int (*Fun) (int);
```

```
class Composer {
```

```
private:
```

```
    const vector<Fun>& funs;
```

```
    static int apply(int sofar, Fun f) {
```

```
        return f(sofar);
```

```
    }
```

```
public:
```

```
    Composer(const vector<Fun>& fs) : funs(fs) {}
```

```
    int operator()(int x) const {
```

```
        return accumulate(funs.rbegin(), funs.rend(),
```

```
            x, apply);
```

```
    }
```

```
};
```


Using compose

```
int add1(int x) {  
    return x + 1;  
}
```

```
int mult3(int x) {  
    return x * 3;  
}
```

```
int sub5(int x) {  
    return x - 5;  
}
```

```
int main() {  
    vector<Fun> funcs;  
    funcs.push_back(add1);  
    funcs.push_back(mult3);  
    funcs.push_back(sub5);  
    Composer comp(funcs);  
    cout << comp(1) << endl; // -11  
    cout << comp(20) << endl; // 46  
}
```

Scala

- A FP front-end to the JVM
 - statically typed
 - type inference
- Pretty much a copy of ML
 - pattern matching
 - **foldright**, **foldleft**, etc.

compose in Scala

```
object Compose {  
  def compose3[T](flist: List[(T) => T]): (T) => T =  
    (x: T) => flist.foldRight(x)  
      ((f: (T) => T,sofar: T) => f(sofar))  
  
  def main(args: Array[String]) {  
    val addOne = (x: Int) => x + 1  
    val addTwo = (x: Int) => x + 2  
    val addThree = (x: Int) => x + 3  
    val addFour = compose(List(addOne, addOne, addOne, addOne))  
    println(addFour(1)) // 5  
    val addSix = compose(List(addOne, addTwo, addThree))  
    println(addSix(1)) // 7  
  }  
}
```

union in Scala

```
object Union {
  def union[T](a: List[T], b: List[T]): List[T] =
    (a, b) match {
      case (x, Nil) => x
      case (x, head :: rest) => {
        if (x contains head)
          union(x, rest)
        else
          head :: union(x, rest)
      }
    }

  def main(args: Array[String]) {
    println(union(List("a", "b", "c"), List("b", "c", "d")))
  }
}
```

FP in C# 3.0

- As in D, *delegates* act as closures
- Lambdas via *anonymous delegates*
- Type inference with **var**

addn in C# 3.0

```
public static Func<int, int> addn(int n)
{
    return new Func<int, int>(x => x + n);
}
```

...

```
var f2 = addn(5);
Console.WriteLine(f2(2));    // 7
```

compose in C# 3.0

```
public static Func<T, T> Compose<T>(IEnumerable<Func<T, T>> funcs)
{
    return new Func<T, T>(i =>
    {
        T result = i;
        foreach (var func in funcs.Reverse())
        {
            result = func(result);
        }
        return result;
    });
}
```

Using compose

```
IEnumerable<Func<int, int>> t = new List<Func<int, int>>
{
    new Func<int, int>(x => x + 1),
    new Func<int, int>(x => x * 3),
    new Func<int, int>(x => x - 5)
};

...
```

```
var c = Compose(t);
Console.WriteLine(c(1));           // -11
Console.WriteLine(c(20));         // 46
```


The Future of FP

D 3.0

- Will add “pure functions”
 - functions that don't change state
- Will add a bunch of algorithms
- Will support full FP and STM (a la Haskell)

Java

- Closures proposal
 - somewhat controversial
- Inner Classes are a poor-man's closure
- Algorithms have been around via JGL for over 10 years

C++0x

- More flexible lambda expressions
- More flexible function-argument binding